POINCARE BREAKING AND GAUGE INVARIANCE:

A ROAD TO EMERGENT GRAVITY AND NEW PARTICLES

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SUMMARY

- \triangleright In effective QFTs with a UV cutoff Λ , all gauge bosons acquire masses in proportion to Λ .
 - \triangleright Gauge symmetries, broken explicitly by Λ , can be restored by invoking "Higgs mechanism".
 - \blacktriangleright The anticipated "Higgs field" must break Poincare symmetry since the cutoff Λ does so.
 - ➤ The "Higgs field" can be linked to curvature as they both break the Poincare symmetry.
 - ➤ Gravity emerges then holographically as a completion of the flat spacetime effective QFT.
- ➤ Proper emergence of gravity brings in a plethora of new particles that do not have to couple to the known ones.

AN ILLUSTRATIVE CASE: SAKHAROV'S INDUCED GRAVITY

- \triangleright Sakharov's setup involves a flat spacetime QFT bordered in the UV by a UV cutoff Λ .
- \blacktriangleright Matter loops are assumed to have a curved metric $g_{\alpha\beta}$, and they can induce gravity therefore if Λ lies at the Planck scale.
- > ... and yet Sakharov's induced gravity comes with all sort of UV sensitivity problems in the QFT sector:

$$S_{ind} = \int d^4x \sqrt{-g} \left\{ -a_R \Lambda^2 R(g) - a_O \Lambda^4 - \sum_m c_m m^2 \Lambda^2 - a_\phi \Lambda^2 \phi^{\dagger} \phi - a_V \Lambda^2 g_{\alpha\beta} \text{tr}[V^{\alpha} V^{\beta}] \right\}$$

Newton's constant

$$(a_R \Lambda^2 \equiv \frac{1}{16\pi G_N})$$

Planckian vacuum energy (cosmological constant problem)

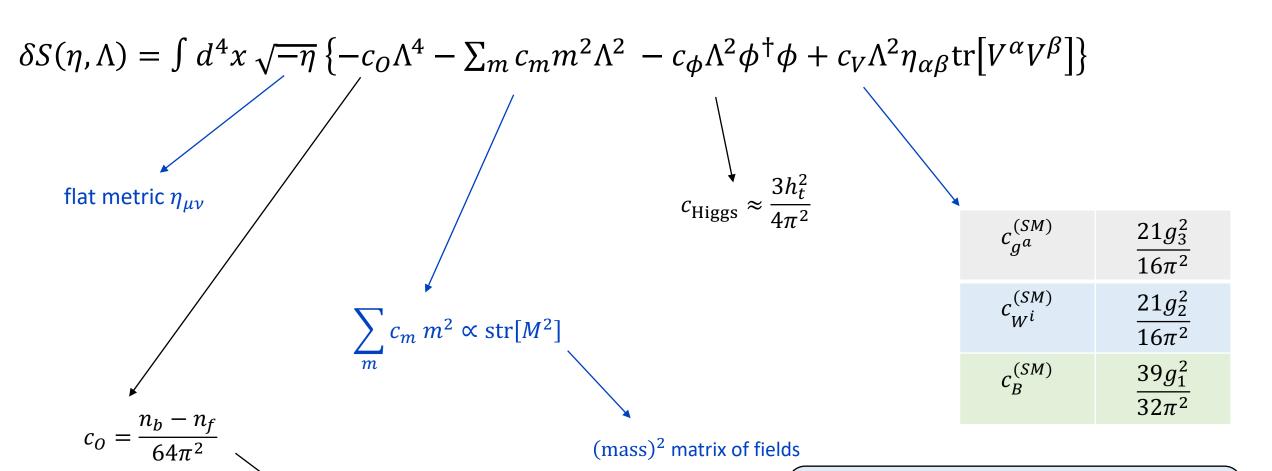
Planckian gauge boson masses (explicit gauge symmetry breaking)

Planckian scalar masses (gauge hierarchy problem)

Can gravity emerge in a way alleviating these problems?

FLAT SPACETIME EFFECTIVE QFT

Quartic and quadratic corrections from matter loops in flat spacetime:



all the bosons (n_b) and fermions (n_f) We may restore gauge symmetries by invoking some sort of "Higgs mechanism".

LOOP-INDUCED GAUGE BOSON MASS TERM

- ightharpoonup Gauge boson anomalous mass term (flat metric): $\delta S_V(\eta,\Lambda) \equiv \int d^4x \sqrt{-\eta} c_V \text{tr}[V^{\alpha} \Lambda^2 \eta_{\alpha\beta} V^{\beta}]$
- Carrying gauge boson mass term to curved spacetime:
 - ☐ Consider these two kinetic structures:

$$I_{V}(\eta) = \int d^{4}x \sqrt{-\eta} \, c_{V} \text{tr} \left[V^{\alpha\beta} V_{\alpha\beta} \right] \xrightarrow{\text{by-parts}} \tilde{I}_{V}(\eta) = \int d^{4}x \sqrt{-\eta} \, c_{V} \text{tr} \left[V^{\alpha} (-D^{2} \eta_{\alpha\beta} + D_{\alpha} D_{\beta} + i V_{\alpha\beta}) V^{\beta} + \partial_{\alpha} \left(V_{\beta} V^{\alpha\beta} \right) \right]$$

☐ Their sensitivity to spacetime curvature enable us to regularize the gauge boson mass term:

$$-I_{V}(\eta) + \tilde{I}_{V}(\eta) = 0 \qquad -I_{V}(g) + \tilde{I}_{V}(g) = -\int d^{4}x \sqrt{-g} c_{V} \text{tr}[V^{\alpha}R_{\alpha\beta}(^{g}\Gamma)V^{\beta}]$$

$$\delta \hat{S}_{V}(g,\Lambda) = -I_{V}(g) + \tilde{I}_{V}(g) + \delta S_{V}(g,\Lambda) = \int d^{4}x \sqrt{-g} c_{V} \text{tr}[V^{\alpha}(\Lambda^{2}g_{\alpha\beta} - R_{\alpha\beta}(^{g}\Gamma))V^{\beta}]$$

$$\delta \hat{S}_{V}(\eta, \Lambda) = -I_{V}(\eta) + \tilde{I}_{V}(\eta) + \delta S_{V}(\eta, \Lambda) = \delta S_{V}(\eta, \Lambda)$$

We proceed with this regularized gauge boson anomalous mass term.

RESTORATION OF GAUGE SYMMETRIES

 \triangleright Mass term for a vector boson V_{μ} (Proca field):

$$S_V(g, M_V) = \int d^4x \sqrt{-g} M_V^2 \eta_{\alpha\beta} \text{tr}[V^{\alpha}V^{\beta}]$$

	M_V^2
Gauge breaking	Yes
Poincare breaking	No

E. Fermi, La Ricerca Scientifica 4, 491 (1933)

H. Yukawa, Proc. Math. Soc. Jpn. 17, 48 (1935)

 \triangleright Loop-induced anomalous mass term for a gauge boson V_{μ} :

$$\delta \hat{S}_V(g,\Lambda) = \int d^4x \sqrt{-g} c_V \text{tr}[V^{\alpha}(\Lambda^2 g_{\alpha\beta} - R_{\alpha\beta}({}^g\Gamma))V^{\beta}]$$

	$\Lambda^2 - R$
Gauge breaking	Yes
Poincare breaking	Yes

H. Umezawa et al., Prog. Theor. Phys. 3, 317 (1948)
G. Kallen, Helv. Phys. Acta. 22, 637 (1949)
M.Peskin & D. Schroeder, Quantum Field Theory (1995)
P. Chankowski et al., Acta Phys. Pol. B48, 5 (2017)

RESTORATION OF GAUGE INVARIANCE

Higgsing massive gauge boson:

$$S_{V}(g, M_{V}) = \int d^{4}x \sqrt{-g} \, M_{V}^{2} g_{\alpha\beta} \mathrm{tr}[V^{\alpha}V^{\beta}]$$

$$M_{V}^{2} \Longrightarrow \text{"spurion } \phi \text{"}$$
(Poincare-conserving)
$$S_{V}(g, \phi) = \int d^{4}x \sqrt{-g} \, g_{\alpha\beta} \mathrm{tr}[\phi^{\dagger}V^{\alpha}V^{\beta}\phi]$$

$$\mathrm{spurion} \Longrightarrow \text{"Higgs}$$

$$S_{V}(g, \phi) = \int d^{4}x \sqrt{-g} \, g_{\alpha\beta} \mathrm{tr}[(D^{\alpha}\phi)^{\dagger}D^{\beta}\phi]$$

P. Anderson, Phys. Rev. Phys. **130**, 439 (1962) F.Englert & R. Brout, Phys. Rev. Lett. **13**, 321 (1964) P. Higgs, Phys. Rev. Lett. **13**, 508 (1964)

Higgsing anomalously massive gauge boson:

$$\delta \hat{S}_{V}(g,\Lambda) = \int d^{4}x \sqrt{-g} c_{V} \operatorname{tr}[V^{\alpha}(\Lambda^{2}g_{\alpha\beta} - R_{\alpha\beta}(^{g}\Gamma))V^{\beta}]$$

$$\Lambda^{2} \Longrightarrow \text{"spurion } \Sigma^{"}$$

$$(\text{Poincare-breaking})$$

$$\delta \hat{S}_{V}(g,\Sigma) = \int d^{4}x \sqrt{-g} c_{V} \operatorname{tr}[V^{\alpha}(\Sigma(x)g_{\alpha\beta} - R_{\alpha\beta}(^{g}\Gamma))V^{\beta}]$$

What is this spurion Σ ? It cannot be $\phi^{\dagger}\phi$ as it cannot break Poincare symmetry! Can it be related to spacetime curvature?

UV CUTOFF AND CURVATURE: POINCARE AFFINITY

➤ In an arbitrary second-quantized theory with no presumed properties, "... lack of translational invariance would just be interpreted as the effect of gravitational fields being present, which are not translational invariant."

C. Froggatt & H. Nielsen, Ann. Phys. **517**, 115 (2007)

 \triangleright Belonging inherently to the flat spacetime, QFTs have one natural Poincare (translation) breaking source: the UV cutoff Λ .

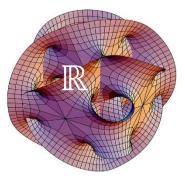
DD, Gen. Rel. Grav. 53, 22 (2021)

 \triangleright On physical grounds, therefore, there is a Poincare affinity between the UV cutoff Λ in flat spacetime and curvature \mathbb{R} in curved spacetime.

DD, Gen. Rel. Grav. 53, 22 (2021)



Poincare affinity



RESTORATION OF GAUGE INVARIANCE

Higgsing massive gauge boson:

$$S_V(g, M_V) = \int d^4x \sqrt{-g} \, M_V^2 g_{\alpha\beta} \mathrm{tr}[V^\alpha V^\beta]$$

$$M_V^2 \Longrightarrow \text{"spurion } q$$
(Poincare-conserving)

$$S_V(g,\phi) = \int d^4x \sqrt{-g} \ g_{\alpha\beta} \mathrm{tr}[\phi^\dagger V^\alpha V^\beta \phi]$$
 spurion \Longrightarrow "Higgs

$$S_V(g,\phi) = \int d^4x \sqrt{-g} g_{\alpha\beta} \text{tr}[(D^{\alpha}\phi)^{\dagger}D^{\beta}\phi]$$

Higgsing anomalously massive gauge boson:

$$\delta \hat{S}_V(g,\Lambda) = \int d^4x \sqrt{-g} c_V \operatorname{tr}[V^\alpha (\Lambda^2 g_{\alpha\beta} - R_{\alpha\beta}(^g\Gamma))V^\beta]$$

$$\Lambda^2 \xrightarrow{\text{"spurion } \Sigma"} \text{(Poincare-breaking)}$$

$$\delta \hat{S}_V(g, \Sigma) = \int d^4x \sqrt{-g} \ c_V \mathrm{tr} [V^\alpha (\Sigma(x) g_{\alpha\beta} - R_{\alpha\beta} (^g\Gamma)) V^\beta]$$

$$\Sigma(x) \ g_{\mu\nu}(x) = \mathbb{R}_{\mu\nu}(\Gamma(x))$$
(affine curvature \mathbb{R})

$$\delta \hat{S}_V(g,\mathbb{R}) = \int d^4$$

 $\delta \hat{S}_V(g,\mathbb{R}) = \int d^4$ We can now form a symmetry-driven Palatini gravity (SPG) theory with the inclusion of non-gauge sectors.

SYMMETRY-DRIVEN PALATINI GRAVITY THEORY

 \blacktriangleright Affine curvature $\mathbb R$ gives rise to SPG gravity via $\Sigma(x)$ $g_{\mu\nu}(x) = \mathbb R_{\mu\nu}(\Gamma(x))$:

$$\delta \hat{S}(g,\mathbb{R}) = \int d^4x \sqrt{-g} \left\{ -\frac{c_O}{16} \left(g^{\alpha\beta} \mathbb{R}_{\alpha\beta}(\Gamma) \right)^2 - \frac{g^{\alpha\beta} \mathbb{R}_{\alpha\beta}(\Gamma)}{16\pi G_N} - \frac{c_\phi}{4} g^{\alpha\beta} \mathbb{R}_{\alpha\beta}(\Gamma) \phi^{\dagger} \phi + c_V(\mathbb{R}_{\alpha\beta}(\Gamma) - R_{\alpha\beta}(g\Gamma)) \operatorname{tr} \left[V^{\alpha} V^{\beta} \right] \right\}$$

 \triangleright Equation of motion for the affine connection $\Gamma_{\alpha\beta}^{\lambda}$ (${}^{\Gamma}\nabla_{\lambda}$ covariant derivative wrt $\Gamma_{\alpha\beta}^{\lambda}$):

$$^{\Gamma}\nabla_{\lambda}Q_{\alpha\beta}=0$$

☐ Field metric:

$$Q_{\alpha\beta} = \left(\frac{1}{16\pi G_N} + \frac{c_S}{4}g^{\alpha\beta}S^{\dagger}S + \frac{c_O}{8}g^{\mu\nu}\mathbb{R}_{\mu\nu}(\Gamma)\right)g_{\alpha\beta} - c_V \text{tr}[V_{\alpha}V_{\beta}]$$

☐ Newton's constant:

$$G_N^{-1} = 4\pi \sum_m c_m m^2 \xrightarrow{\text{1-loop}} 4\pi \, \text{str}[M^2]$$

Now, we integrate out the affine connection $\Gamma_{\mu\nu}^{\lambda}$ to determine the resulting metrical gravity theory.

INTEGRATING-OUT THE AFFINE CONNECTION

> General solution for the affine connection:

$$\Gamma_{\alpha\beta}^{\lambda} = {}^{g}\Gamma_{\alpha\beta}^{\lambda} + \frac{1}{2}(Q^{-1})^{\lambda\rho} (\nabla_{\alpha}Q_{\beta\rho} + \nabla_{\beta}Q_{\rho\alpha} - \nabla_{\rho}Q_{\alpha\beta})$$

 \triangleright Enormity of the Planck scale $G_N^{-1/2}$ leads to:

$$\Box \Gamma_{\alpha\beta}^{\lambda} = {}^{g}\Gamma_{\alpha\beta}^{\lambda} + 8\pi G_{N} (\nabla_{\alpha}Q_{\beta}^{\lambda} + \nabla_{\beta}Q_{\alpha}^{\lambda} - \nabla^{\lambda}Q_{\alpha\beta}) + \mathcal{O}(G_{N}^{2})$$

$$\square \quad \mathbb{R}_{\alpha\beta}(\Gamma) = R_{\alpha\beta}({}^{g}\Gamma) + 8\pi G_{N} \left(\nabla^{\mu}\nabla_{\alpha}\delta^{\nu}_{\beta} + \nabla^{\nu}\nabla_{\alpha}\delta^{\mu}_{\beta} - \square\delta^{\mu}_{\alpha}\delta^{\nu}_{\beta} - \nabla_{\alpha}\nabla_{\beta}g^{\mu\nu} + (\alpha \leftrightarrow \beta) \right) Q_{\mu\nu} + \mathcal{O}(G_{N}^{2})$$

derivatives of the scalars ϕ and gauge fields V_i^lpha

EMERGENCE OF THE GR FROM RESTORATION OF GAUGE SYMMETRIES

Integration-out of $\mathbb{R}_{\alpha\beta}(\Gamma)$ reduces SPG to the GR $(R(g) = g^{\alpha\beta}R_{\alpha\beta}({}^g\Gamma))$:

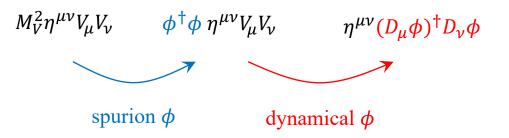
gauge symmetries got restored!

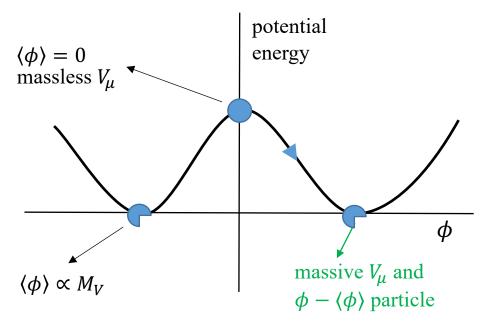
GR emerged!

quadratic UV sensitivity of scalar masses gives cause to curvaturescalar fields couplings

quartic UV sensitivity in flat spacetime gives cause to quadratic curvature terms

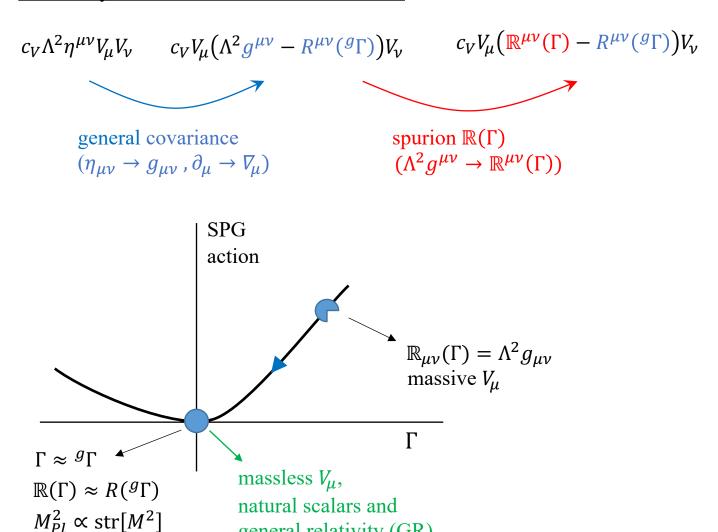
Summary: Higgs Mechanism





- Max of energy \Rightarrow massless V_{μ} (exact gauge symmetry)
- \bigcirc Min of energy \Rightarrow massive V_{μ} (broken gauge symmetry)

Summary: Affine Curvature Mechanism



- ho Non-extrema of SPG action \Rightarrow anam. massive V_{μ} (broken gauge symmetry)
- Extremum of SPG action \Rightarrow massless V_{μ} (exact gauge symmetry and GR)

general relativity (GR)

RENORMALIZED QFT + EMERGENT GRAVITY:

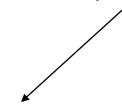
$$S_{QFT+GR} = S(g, \psi) + \delta S(g, \psi) + \int d^4x \sqrt{-g} \left\{ -\frac{R(g)}{16\pi G_N} - \frac{c_O}{16} R(g)^2 - \frac{c_\phi}{4} R(g) \phi^{\dagger} \phi + \mathcal{O}(G_N) \right\}$$

QFT with

- dimensional-regularization in the classical curved background geometry,
- loop corrections computed in the flat spacetime QFT

$$R + R^2$$
 gravity with

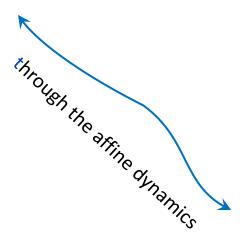
- non-minimal coupling to scalars,
- $\mathcal{O}(G_N)$ remainder involving derivatives of scalars and gauge fields,
- loop-induced coefficients computed in the flat spacetime QFT.



HOLOGRAPHIC STRUCTURE

Energy density in flat spacetime:

$$c_0 \Lambda^4 + c_m m^2 \Lambda^2 + c_\phi \Lambda^2 \phi^{\dagger} \phi + c_V \Lambda^2 \text{tr}[V^{\alpha} V_{\alpha}]$$



Curvature sector ($\Lambda_{IR}^2 \propto R$):

$$\left(\frac{1}{8\pi G_N} + \cdots\right) R = \frac{c_O}{16} R^2 + \frac{R}{8\pi G_N} + \frac{c_\phi}{4} R \phi^{\dagger} \phi$$

PREDICTIONS OF THE SYMMERGENT GRAVITY

new massive particles are a must for Newton's constant to take right value

neutrinos must be Dirac for the Higgs mass to remain stable

black hole shadow, photon radius and quasiperiodic oscillations show distinctive features

dark matter must couple with a strength $\leq m_h^2/m_{DM}^2$ to known particles for the Higgs mass to remain stable

Higgs-curvature coupling is about 10 % in the SM, and deviations indicate Higgs coupling to new particles

detection of new particles can wait for high-luminosity LHC

pure Einstein gravity is attained if bosons and fermions are equal in number

cosmic inflation is expected to be of Starobinsky type

DD, Adv. High Energy Phys. 6727805 (2016)

DD, Adv. High Energy Phys. 4652048 (2019)

DD, Gen. Rel. Grav. 53, 22 (2021)

K. Cankocak et al., Eur. Phys. J. C80, 1188 (2020)

DD & C. S. Ün, arXiv: 2005.03589 [hep-ph] (2020)

DD, Galaxies 9, 2 (2021)

I. Çimdiker, Phys. Dark Universe 30, 100736 (2020)

DD, B. Pulice & N. Sönmez, work in progress (2022)

I. Çimdiker, DD & A. Övgün, Phys. Dark Univ. **34**, 100900 (2021)

J. Rayimbayev, R. Pantig, A. Övgün, A. Abdujabbarov & DD, arXiv: 2206.06599 [gr-qc]

R. Pantig, A. Övgün & DD, arXiv: <u>2208.02969</u> [gr-qc]

GRAZIE MILLE!

BACK UP SLIDES 1

REALIZING POINCARE AFFINITY: DETACHMENT OF POWER-LAWS AND LOGARITHMICS

- $ightharpoonup \log \Lambda$ corrections to particle masses can cause equivalence principle violation under the Poincare affinity $\Lambda^2 \Rightarrow \mathbb{R}(x)$.
- > This violation can be prevented by detaching power-law and logarithmic corrections so that:
 - power-laws involve Λ
 - logarithmics involve a different scale μ
- > The detached regularization can be constructed as an extension of the dimensional regularization:
 - DimReg continues loop amplitudes from 4 to D momentum space dimensions (n = 0,1,2)

$$I_n = \int \frac{d^4p}{(2\pi)^4} \frac{1}{(p^2 - m^2 + i0)^n} \quad \Longrightarrow \quad \mu^{4-D} \int \frac{d^Dp}{(2\pi)^D} \frac{1}{(p^2 - m^2 + i0)^n}$$

and comprises logarithmic, quadratic and quartic divergences as $D \to 4$, $D \to 2$ and $D \to 0$.

What is the function $f(\Lambda, \mu; D, \pi)$? I. Jack & D. Jones, Nucl. Phys. **B342**, 127 (1990); M. Al-Sarhi, D. Jones & I. Jack, Nucl. Phys. **B345**, 431 (1990)

DimReg can be extended to form the Detached Regularization:

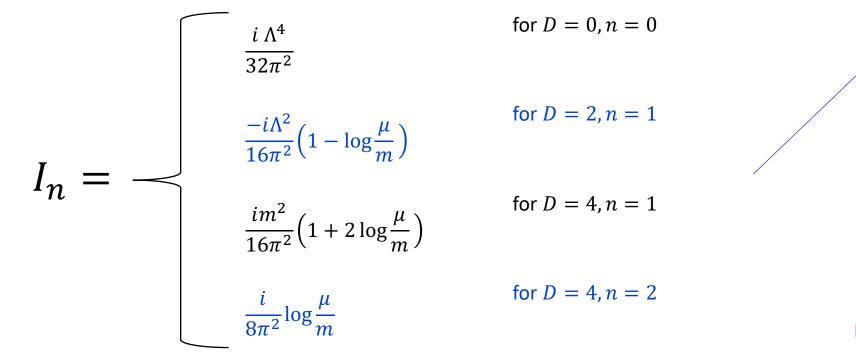
$$I_n = \mu^{4-D} \int \frac{d^D p}{(2\pi)^D} \frac{1}{(p^2 - m^2 + i0)^n} \longrightarrow f(\Lambda, \mu; D, n) \int \frac{d^D p}{(2\pi)^D} \frac{1}{(p^2 - m^2 + i0)^n}$$

REALIZING POINCARE AFFINITY: DETACHMENT OF POWER-LAWS AND LOGARITHMICS

ightharpoonup If Λ —dependence is to reminesence the cutoff regularization and if DimReg results are to remain unchanged then the function $f(\Lambda, \mu; D, n)$ must have the form:

$$f(\Lambda, \mu; D, n) = \left(\frac{8 - 2D}{8 - D^2}\right)^2 \frac{1}{(8\pi)^{2-n}} \Lambda^{4-2n} \mu^{2n-D} + \left(\frac{D(D-2)(16 - 3D)}{32}\right)^2 \mu^{4-D}$$
vanishes as $D \to 4$ vanishes as $D \to 0$ and $D \to 2$

 \triangleright Then, in the \overline{MS} renormalization scheme, the loop amplitudes take the detached form:



Detached regularization:

- Λ for <u>power-law</u> corrections
- μ for <u>logarithmic</u> corrections

DD, talk at Gravitex21 (2021) DD, talk at FFP16 (2022) DD, C. Karahan & O. Sargın, submitted (2022)

BACK UP SLIDES 2

STANDARD MODEL OF ELEMENTARY PARTICLES

SUCCESSES

- SM is a renormalizable QFT of the strong, weak and electromagnetic interactions.
- SM agrees with all the existing experimental data.
- > SM is a natural QFT in isolation.

PROBLEMS

- ➤ SM cannot account for empirical facts like galactic flat rotation curves, neutrino masses, baryon asymmetry, inflation, and neutron magnetic moment.
- SM Higgs sector is destabilized by high-scale physics.

 (e.g. Heavy RH neutrinos generating the neutrino Majorana masses destable destabilized by high-scale physics.
 - 1. Give priority to gravity.
- SM does not involve g (Basically, GR is not a G. 't Hooft & M. Veltman,
- 2. Study other problems in the setup involving gravity.

THE SM DOESN'T ACCORD WITH GRAVITY BECAUSE ...

➤ GR is not a renormalizable QFT.

G. 't Hooft & M. Veltman, Ann. de I.H.P 20, 69 (1974)M. Goroff & A. Sagnotti, NPB 266, 709 (1986)

➤ Classical GR is not eligible since QFTs (like the SM) are inherently specific to the flat spacetime with their Poincare-invariant vacuum states. They cannot thus be continued to curved spacetime.

S. Hollands & R. Wald, Phys. Rep. **574**, 1 (2015)

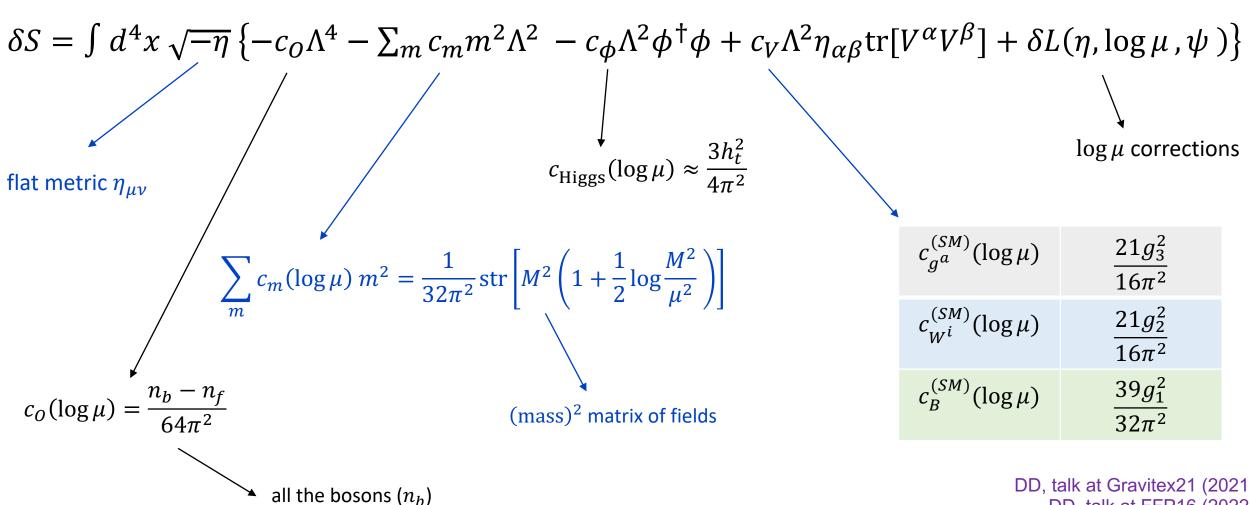
C. Gerard, arXiv: 1901.10175 (2019)

Strings, LQG, asymptotic safety, causal dynamical triangulations and others are currently "work in progress". But the SM may accord with induced/emergent gravity as it arises from the matter loops.

REALIZING POINCARE AFFINITY: EFFECTIVE ACTION IN DETACHED REGULARIZATION

Quantum corrections involve powers of Λ with $\log \mu$ – dependent loop factors:

and fermions (n_f)



DD, talk at Gravitex21 (2021) DD, talk at FFP16 (2022) DD, C. Karahan & O. Sargın, submitted (2022)

AFFINE CURVATURE AS THE POINCARE-BREAKING SPURION

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